

MIT CSAIL



6.819 / 6.869 : Advances in Computer Vision

Bill Freeman and Antonio Torralba, 2017

### Lecture 18 Nov. 9, 2017

### **Belief Propagation and Graphical Models**





### Identical local evidence...



### ...different interpretations







# Information must propagate over the image.



Probabilistic graphical models are a powerful tool for propagating information within an image. And these tools are used everywhere within computer vision now. http://www.cvpapers.com/cvpr2014.html

From a random sample of 6 papers from CVPR 2014, half had figures that look like this... Partial Optimality by Pruning for MAP-inference with General Graphical Models, Swoboda et al



Figure 1. An exemplary graph containing inside nodes (yellow with crosshatch pattern) and boundary nodes (green with diagonal pattern). The blue dashed line encloses the set A. Boundary edges are those crossed by the dashed line.

http://hci.iwr.uni-heidelberg.de/Staff/bsavchyn/papers/swoboda-GraphicalModelsPersistency-with-Supplement-cvpr2014.pdf Active flattening of curved document images via two structured beams, Meng et al.



Figure 5. The directed graph G for computing the correspondence function. (a) discretization of the t-s plane, (b) the constructed graph. All the vertices of the graph locate in a parallelogram. The slops of its edges are a and b, respectively.

file:///Users/billf/Downloads/dewarp\_high.pdf 9

#### A Mixture of Manhattan Frames: Beyond the Manhattan World, Straub et al



Figure 3: Graphical model for a mixture of K MFs.

http://www.jstraub.de/download/straub2014mmf.pdf

### MRF nodes as patches



### Network joint probability



## Energy formulation

$$E(x,y) = k + \sum_{(i,j)} \beta(x_i, x_j) + \sum \alpha(x_i, y_i)$$

$$inage$$

$$Scene-scene compatibility function$$

$$Scene-scene compatibility function$$

$$Image-scene compatibil$$

## Outline of MRF section

- Inference in MRF's.
  - Gibbs sampling, simulated annealing
  - Iterated conditional modes (ICM)
  - Loopy belief propagation
    - Application example—super-resolution
  - Graph cuts
  - Variational methods
- Learning MRF parameters.
  - Iterative proportional fitting (IPF)

Belief, and message update rules are just local operations, and can be run whether or not the network has loops

$$\mathbf{j} \qquad b_j(x_j) = \prod_{k \in N(j)} M_j^k(x_j)$$

$$M_{i}^{j}(x_{i}) = \sum_{x_{j}} \Psi_{ij}(x_{i}, x_{j}) \prod_{k \in \mathcal{N}(j) \setminus i} M_{j}^{k}(x_{j})$$

$$\mathbf{i} = \mathbf{i} = \mathbf{j}$$

$$\mathbf{j} = \mathbf{j}$$
15

Justification for running belief propagation in networks with loops

- Experimental results:
  - Comparison of methods Szeliski et al. 2008 http://vision.middlebury.edu/MRF/
  - Error-correcting codes Kschischang and Frey, 1998;
     McEliece et al., 1998
  - Vision applications

Freeman and Pasztor, 1999; Frey, 2000

- Theoretical results:
  - For Gaussian processes, means are correct. Weiss and Freeman, 1999
  - Large neighborhood local maximum for MAP.
     Weiss and Freeman, 2000
  - Equivalent to Bethe approx. in statistical physics. Yedidia, Freeman, and Weiss, 2000
  - Tree-weighted reparameterization

Wainwright, Willsky, Jaakkola, 2001

# Show program comparing some methods on a simple MRF

testMRF.m

## Outline of MRF section

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## Super-resolution

- Image: low resolution image
- Scene: high resolution image

ultimate goal...



Pixel-based images are not resolution independent



### Pixel replication





Cubic spline, sharpened









Polygon-based graphics images are resolution independent Training-based super-resolution





# 3 approaches to perceptual sharpening

- (1) Sharpening; boost existing high frequencies.
- (2) Use multiple frames to obtain higher sampling rate in a still frame
- (3) Estimate high frequencies not present in image, although implicitly defined.
  - In this talk, we focus on (3), which we'll call "super-resolution".





## Super-resolution: other approaches

- Schultz and Stevenson, 1994
- Pentland and Horowitz, 1993
- fractal image compression (Polvere, 1998; Iterated Systems)
- astronomical image processing (eg. Gull and Daniell, 1978; "pixons" <u>http://casswww.ucsd.edu/puetter.html</u>)
- Follow-on: Jianchao Yang, John Wright, Thomas S. Huang, Yi Ma: Image super-resolution as sparse representation of raw image patches. CVPR 2008

### Training images, ~100,000 image/scene patch pairs

Images from two Corel database categories: "giraffes" and "urban skyline".



### Do a first interpolation



Zoomed low-resolution



Low-resolution



Zoomed low-resolution



Full frequency original



Low-resolution

#### Zoomed low-freq.

### Representation

#### Full freq. original





#### Zoomed low-freq.

### Representation

#### Full freq. original



#### True high freqs

Low-band input (contrast normalized, PCA fitted)

(to minimize the complexity of the relationships we have to learn, we remove the lowest frequencies from the inpu≹7mage, and normalize the local contrast level).

### Gather ~100,000 patches



### Nearest neighbor estimate

Input low freqs.



### Nearest neighbor estimate

Input low freqs.



# Example: input image patch, and closest matches from database

### Input patch



Closest image patches from database

Corresponding high-resolution patches from database







Underlying candidate scene patches. Each renders to the image

## Scene-scene compatibility function, $\Psi(x_i, x_i)$

### Assume overlapped regions, d, of hi-res. patches differ by Gaussian observation noise:

$$\Psi(x_i, x_j) = \exp^{-|d_i - d_j|^2/2\sigma^2}$$



Uniqueness constraint, 33

Image-scene compatibility function,  $\Phi(x_i, y_i)$ 

Assume Gaussian noise takes you from observed image patch to synthetic sample:

$$\Phi(x_i, y_i) = \exp^{-|y_i - y(x_i)|^2/2\sigma^2}$$

V

Χ

### Markov network



### **Belief Propagation**

After a few iterations of belief propagation, the algorithm selects spatially consistent high resolution interpretations for each low-resolution patch of the input image.

Input





Iter. 0

Iter. 1

Iter. 3

## Zooming 2 octaves



We apply the super-resolution algorithm recursively, zooming up 2 powers of 2, or a factor of 4 in each dimension.

85 x 51 input



Cubic spline zoom to 340x204

Max. likelihood zoom  $to^{37}340x204$ 



Original 50x58 Now we examine the effect of the prior assumptions made about images on the high resolution reconstruction. First, cubic spline interpolation.

(cubic spline implies thin plate prior)





True 200x232

#### Original 50x58



(cubic spline implies thin plate prior)







True 200x232

Cubic spline

Next, train the Markov network algorithm on a world of random noise images.



Training images



Original 50x58



The algorithm learns that, in such a world, we add random noise when zoom to a higher resolution.



Training images



Original 50x58

#### Markov network







Original 50x58

### Next, train on a world of vertically oriented rectangles.



#### Training images



Original 50x58

Markov

network



The Markov network algorithm hallucinates those vertical rectangles that it was trained on.



Training images



### Now train on a generic collection of images.

Training images



Original 50x58





Original 50x58

Markov

network

The algorithm makes a reasonable guess at the high resolution image, based on its training images.



Training images





True

## Generic training images









Next, train on a generic set of training images. Using the same camera as for the test image, but a random collection of photographs.



Markov

training:

generic

net,



#### Cubic Spline

True 280x280

### Kodak Imaging Science Technology Lab test.



3 test images, 640x480, to be zoomed up by 4 in each dimension.

8 judges, making 2-alternative, forced-choice comparisons.





## Algorithms compared

- Bicubic Interpolation
- Mitra's Directional Filter
- Fuzzy Logic Filter
- Vector Quantization
- VISTA



Bicubic spline

Altamira

VISTA









Bicubic spline

Altamira

VISTA

## User preference test results

"The observer data indicates that six of the observers ranked Freeman's algorithm as the most preferred of the five tested algorithms. However the other two observers rank Freeman's algorithm as the least preferred of all the algorithms....

Freeman's algorithm produces prints which are by far the sharpest out of the five algorithms. However, this sharpness comes at a price of artifacts (spurious detail that is not present in the original scene). Apparently the two observers who did not prefer Freeman's algorithm had strong objections to the artifacts. The other observers apparently placed high priority on the high level of sharpness in the images created by Freeman's algorithm." Input



Cubic spline zoom

Super-resolution zoom

True high-resolution image







Source image patches

Bandpass filtered and contrast normalized

True high resolution pixels

High resolution pixels chosen by super-resolution

Bandpass filtered and contrast normalized best match patches from training data

> Best match patches from training data



#### Training images



#### Super-resolution zoom

## Training image

angilleyallybiended,or com anelvacatedarulingbythefe ystem,andsentitdowntoanew finedastandardforweighing eraproduct-bundlingdecisi softsaysthatthenewfeature: andpersonalidentification: psoft'sview,butusersandth adedwithconsumerinnovatio rePCindustryislookingforw

## Processed image



### code available online

#### http://people.csail.mit.edu/billf/project%20pages/sresCode/ Markov%20Random%20Fields%20for%20Super-Resolution.html



#### **Markov Random Fields for Super-Resolution**

William T. Freeman	Ce Liu
Massachusetts Institute of Technology	Microsoft Research New England

#### [Download the package]

This is an implementation of the example-based super-resolution algorithm of [1]. Although the applications of MSFs have now extended beyond example-based super resolution and texture synthesis, it is still of great value to revisit this problem, especially to share the source code and examplar images with the research community. We hope that this software package can help to understand Markov random fields for low-level vision, and to create benchmark for super-resolution algorithms.

When you refer to this code in your paper, please cite the following book chapter:

W. T Freeman and C. Liu. Markov Random Fields for Super-resolution and Texture Synthesis. In A. Blake, P. Kohli, and C. Rother, eds., Advances in Markov Random Fields for Vision and Image Processing, Chapter 10. MIT Press, 2011. To appear.

#### Algorithm

The core of the algorithm is based on [1]. We collect pairs of low-res and high-res image patches from a set of images as training. An input low-res image is decomposed to overlapping patches on a grid, and the inference problem is to find the high-res patches from the training database for each low-res patch. We use the kd-tree algorithm, which has been used for real-time texture synthesis [2], to retrieve a set of high-res, k-nearest neighbors for each low-res patch. Lastly, we run a max-product belief propagation (BP) algorithm to minimize an objective function that balances both local compatibility and spatial smoothenss.

#### Examples

Several examples of applying the example-based super resolution code in the package are shown below. These examplar images are also included in the package. Once you run the code, it should give you the same result.

We first apply bicubic sampling to enlarge the input image (a) by a factor of 4 (b), where image details are missing. If we use the nearest neighbor for each low-res patch independently, we obtain high-res but noisy results in (c). To address this issue, we incorporating spatial smoothness into a Markov Random Fields formulation by enforcing the synthesized neighboring patches to agree on the overlapped areas. Max-product belief propagation is used to obtain high-res images in (d). The inferred high-frequency images are shown in (e), and the original high-res are shown in (f).

## Motion application



# What behavior should we see in a motion algorithm?

- Aperture problem
- Resolution through propagation of information
- Figure/ground discrimination

## The aperture problem

http://web.mit.edu/persci/demos/Motion&Form/demos/one-square/one-square.html



## The aperture problem



## motion program demo

#### Inference:

Motion estimation results (maxima of scene probability distributions displayed)

# Image data



Iterations 0 and 1

Initial guesses only show motion at edges.

#### Motion estimation results (maxima of scene probability distributions displayed)



Iterations 2 and 3

Figure/ground still unresolved here.

#### Motion estimation results (maxima of scene probability distributions displayed)



Iterations 4 and 5

Final result compares well with vector quantized true (uniform) velocities.