$\bigcirc$ 

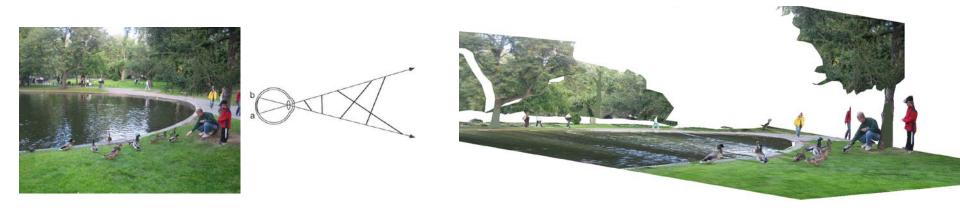
MIT CSAIL

6.869: Advances in Computer Vision

MIT COMPUTER VISION

### Lecture 13 Shape from X

### Depth Perception: The inverse problem



# Monocular cues to depth

- Absolute depth cues: (assuming known camera parameters) these cues provide information about the absolute depth between the observer and elements of the scene
- Relative depth cues: provide relative information about depth between elements in the scene (this point is twice as far at that point, ...)

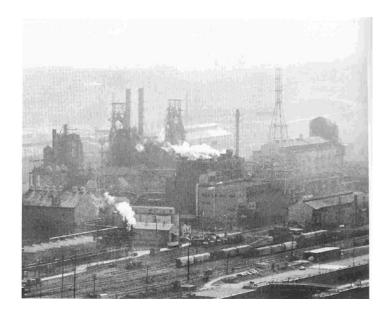
## Relative depth cues



Simple and powerful cue, but hard to make it work in practice...

# Atmospheric perspective

- Based on the effect of air on the color and visual acuity of objects at various distances from the observer.
- Consequences:
  - Distant objects appear bluer
  - Distant objects have lower contrast.



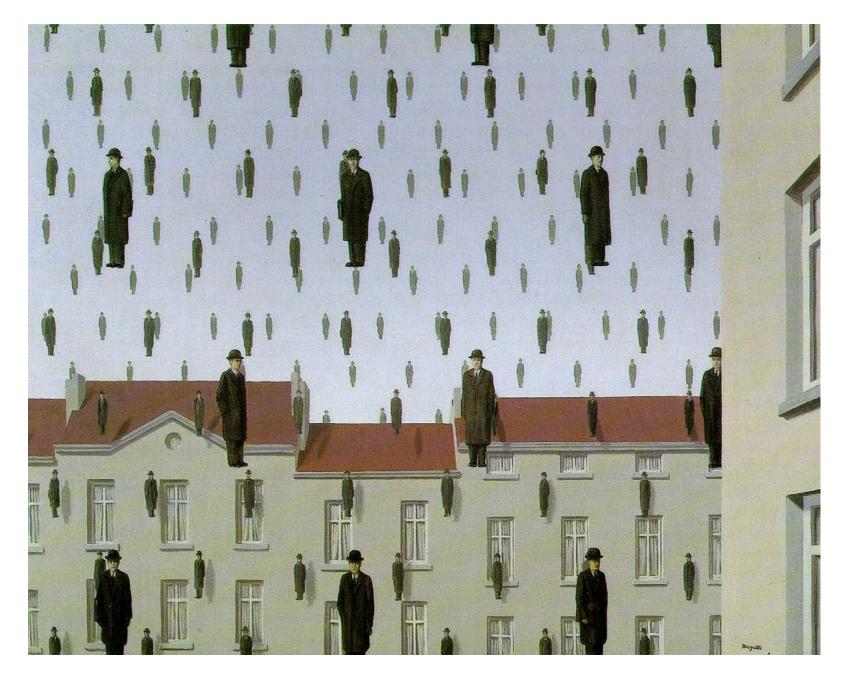
## Atmospheric perspective



http://encarta.msn.com/medias\_761571997/Perception\_(psychology).html



<u>Claude Lorrain</u> (artist) French, 1600 - 1682 Landscape with Ruins, Pastoral Figures, and Trees, 1643/1655



#### [Golconde Rene Magritte]

## Shadows



Cornell CS569 Spring 2008



Lecture 8 • 3

Slide by Steve Marschner

http://www.cs.cornell.edu/courses/cs569/2008sp/schedule.stm

## Shadows

video

## Shadows



http://vision.psych.umn.edu/users/kersten/kersten-lab/shadows.html

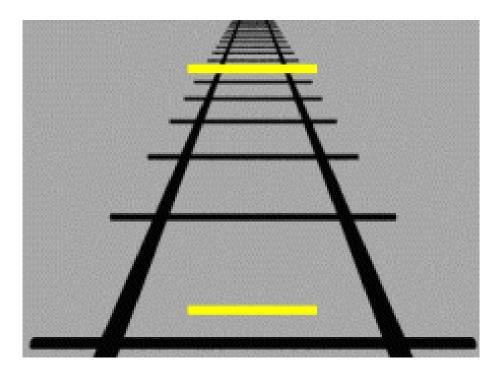
Based on the apparent convergence of parallel lines to common vanishing points with increasing distance from the observer.

(Gibson : "perspective order")

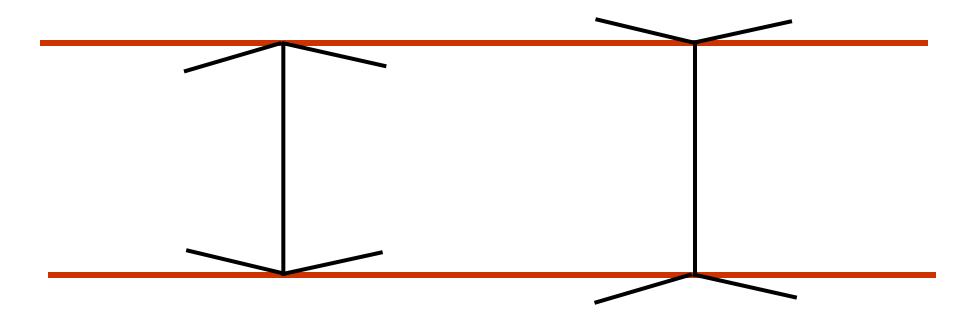
- In Gibson's term, perspective is a characteristic of the visual field rather than the visual world. It approximates how we see (the retinal image) rather than what we see, the objects in the world.
- Perspective : a representation that is specific to one individual, in one position in space and one moment in time (a powerful immediacy).
- Is perspective a universal fact of the visual retinal image ? Or is perspective something that is learned ?



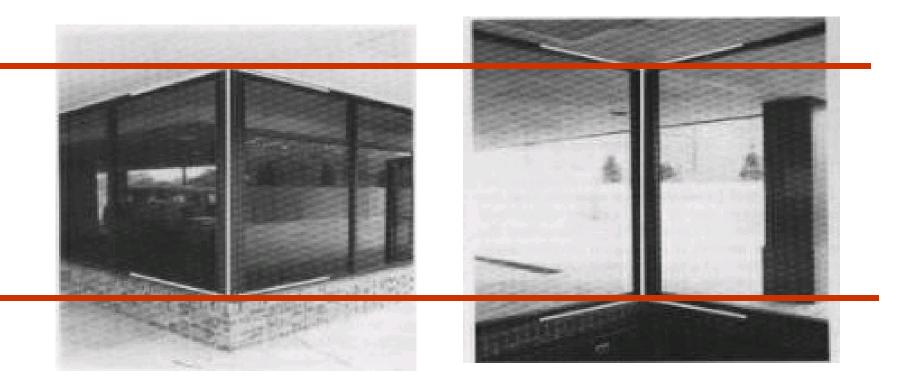
Simple and powerful cue, and easy to make it work in practice...



Ponzo's illusion



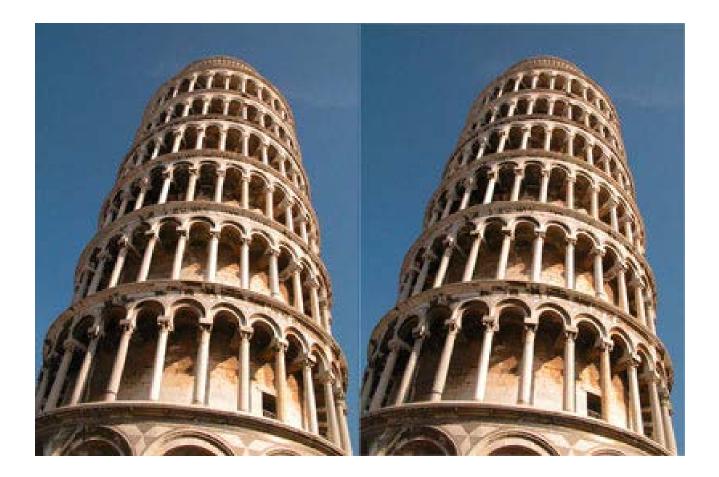
Muller-Lyer 1889



Muller-Lyer 1889

Muller-Lyer 1889

### The two Towers of Pisa



Frederick Kingdom, Ali Yoonessi and Elena Gheorghiu of McGill Vision Research unit.

# The strength of linear perspective



3D percept is driven by the scene, which imposes its ruling to the objects

# Manhattan assumption

#### Application of the statistics of edges: Manhattan World



Many scenes of man-made environments are laid out on a 3-D "Manhattan" grid.

This 3-D structure imposes statistical regularities on the edges, and hence the image gradients, in the image.

These regularities allow us to infer the viewer orientation relative to the Manhattan grid and to detect targets *unaligned* to the grid.

J. Coughlan and A.L. Yuille. "Manhattan World: Orientation and Outlier Detection by Bayesian Inference." Neural Computation. May 2003.

Slide by James Coughlan

#### **Bayesian Model of Manhattan World**

Evidence for line edges -- x, y, z or random lines -- provided by the image gradient. Prior on occurrence of these edges.

**Image gradient magnitude** provides evidence for presence or absence of edges, using  $P_{on}$  and  $P_{off}$  distributions.

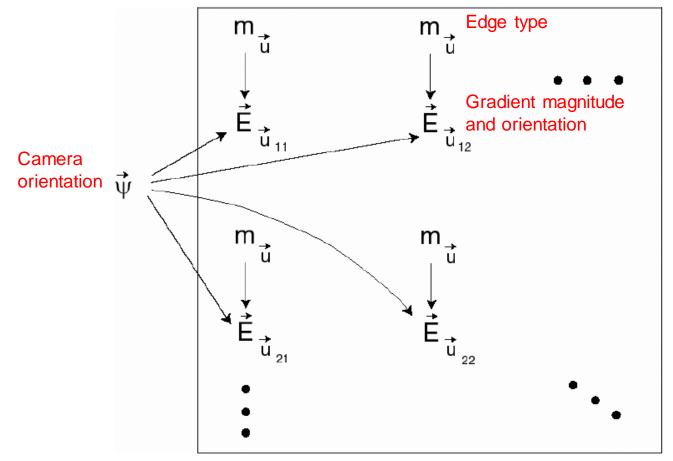
**Image gradient direction** provides information about edge *orientations*.

**Hidden assignment variables:** at each pixel, is there an x, y, z or random line, or no edge at all?

If we knew this assignment at each pixel, and the camera orientation  $\Psi$ , we could predict likely values of image gradient magnitude and direction,  $\vec{E}_{\vec{u}} = (E_{\vec{u}}, \phi_{\vec{u}})$ 

Slide by James Coughlan

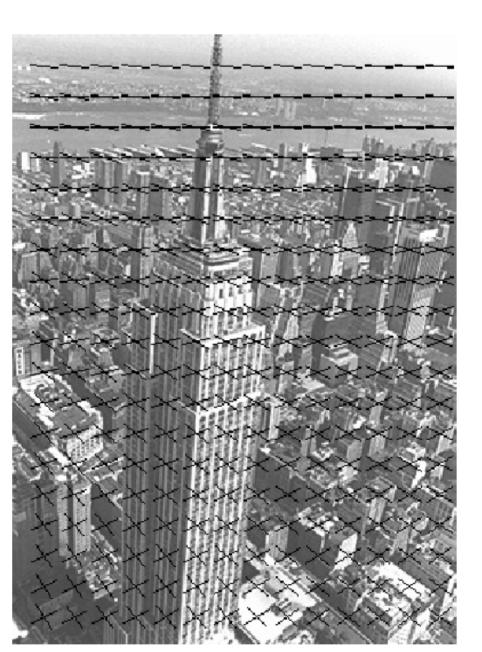
Evidence over all pixels: Bayes net of full Bayesian model



Box represents entire image, with an image gradient vector and assignment variable at each pixel location  $\vec{u}_{ii}$ 

Structure of net graphically illustrates assumption of conditional independence across pixels. Slide by James Coughlan

#### **Experimental Results**

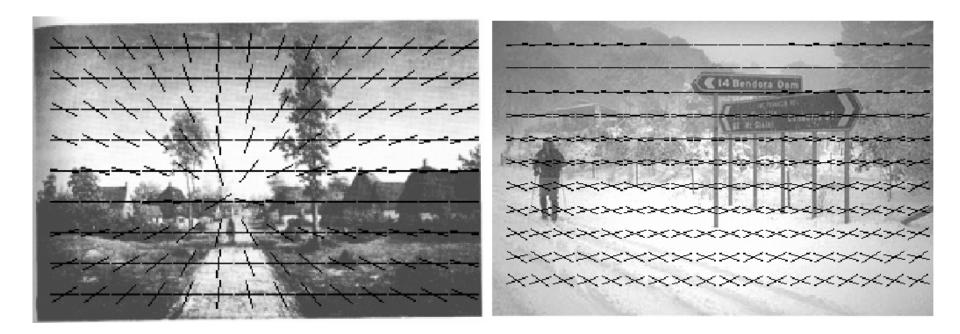


Estimate of *most probable camera orientation given image*, rendered in terms of the corresponding orientations of x and y lines (drawn in black).

Note how the x lines align with the sides of buildings that are visible and facing left. The y lines align with the other visible sides facing right.

Slide by James Coughlan

+ A. A. ++++++++ ++ + + 2 -+ + + + 1 A + + + + + + + 7 × ++++ + 7 × 2 1

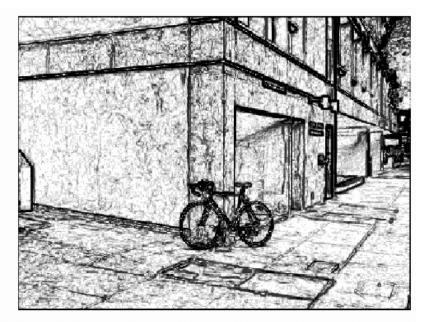


#### **Outlier detection**

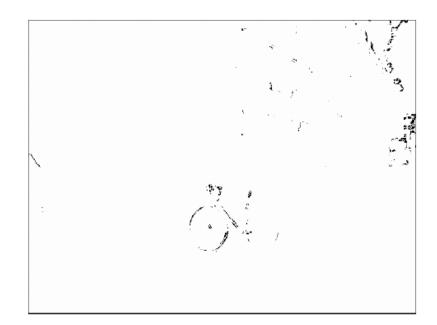
#### Slide by James Coughlan



#### Input image:



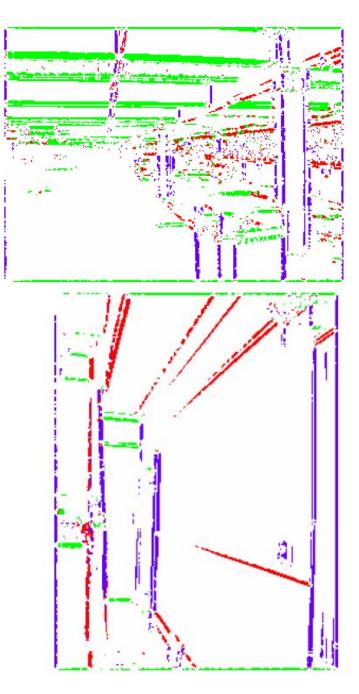
 $Log(P_{on}/P_{off})$ 



#### Outliers detected





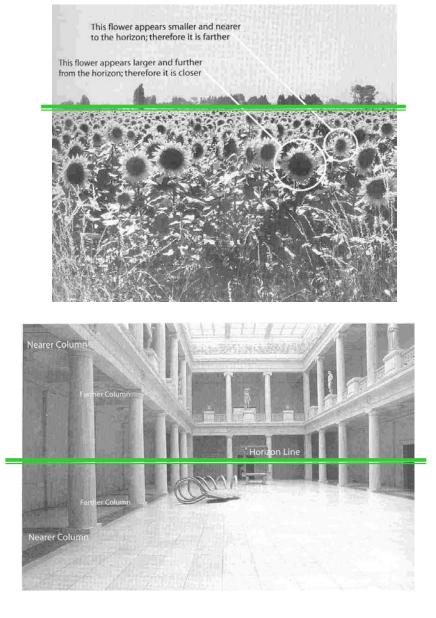


x lines in **red** y lines in **green** z lines in **blue** 

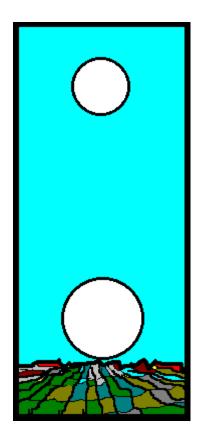
## The importance of the horizon line

### Distance from the horizon line

- Based on the tendency of objects to appear nearer the horizon line with greater distance to the horizon.
- Objects approach the horizon line with greater distance from the viewer. The base of a nearer column will appear lower against its background floor and further from the horizon line. Conversely, the base of a more distant column will appear higher against the same floor, and thus nearer to the horizon line.



# Moon illusion

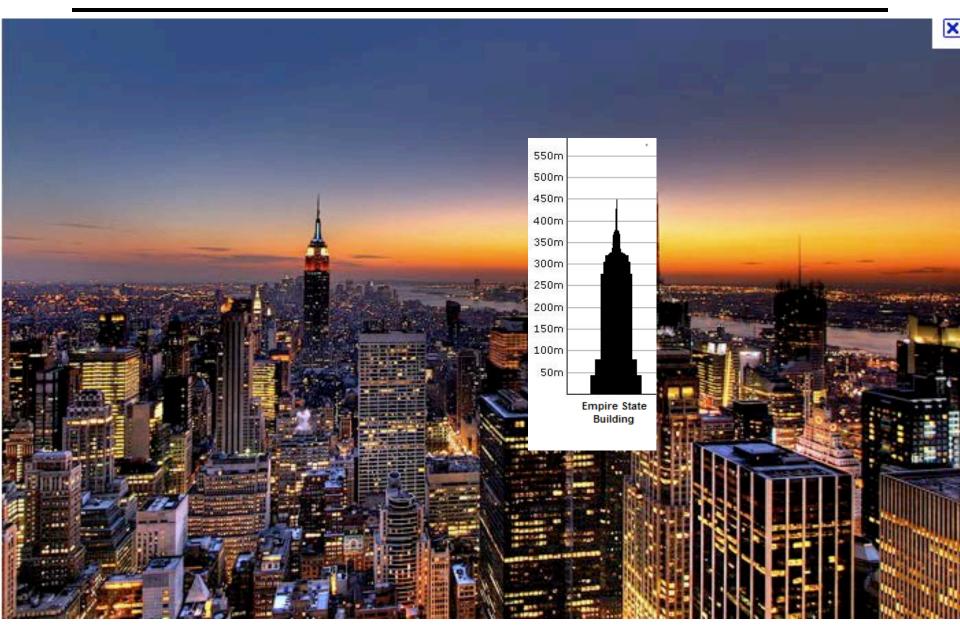


# Relative height

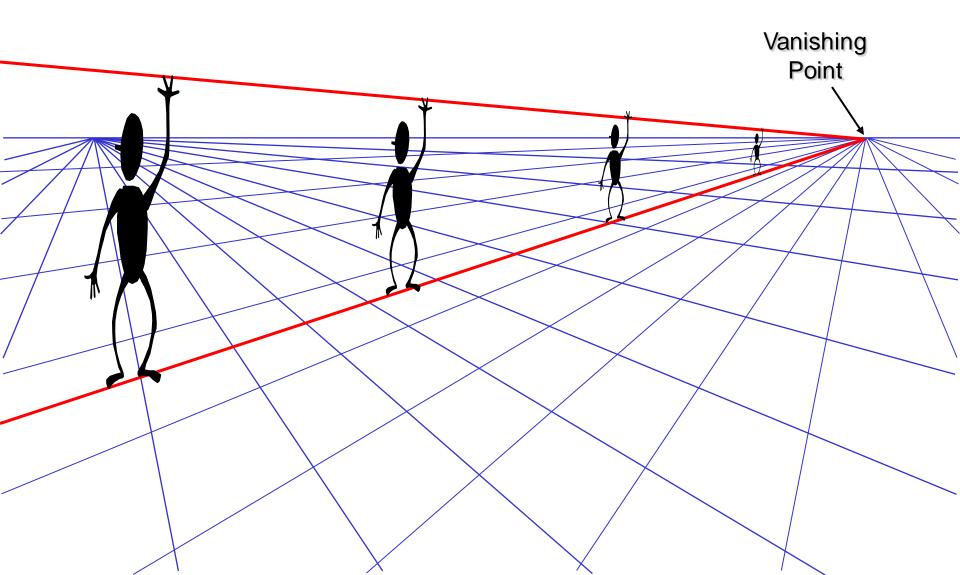
The object closer to the horizon is perceived as farther away, and the object further from the horizon is perceived as closer

If you know camera parameters: height of the camera, then we know real depth

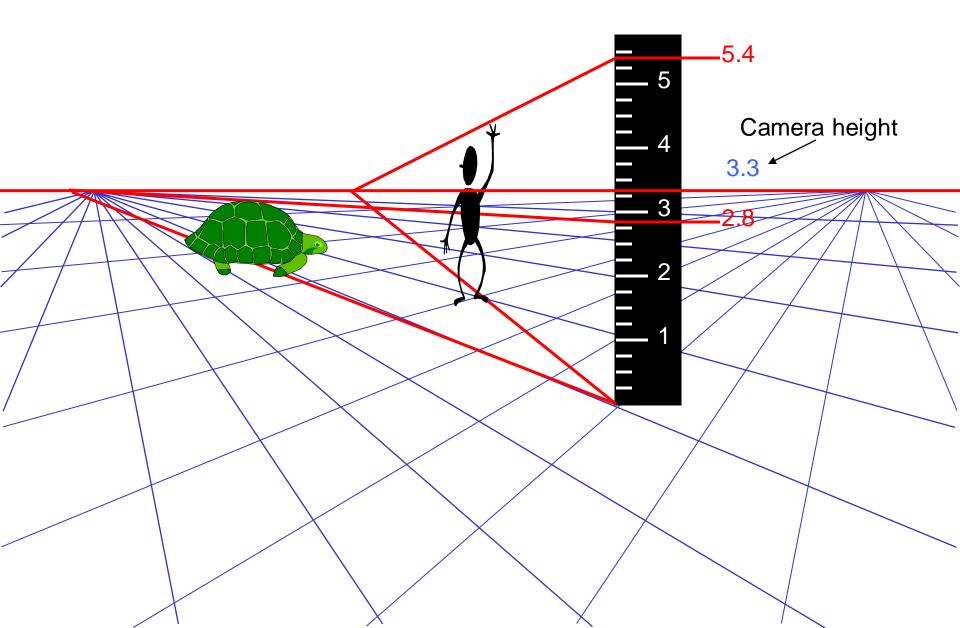
### At which elevation has been taken this picture?



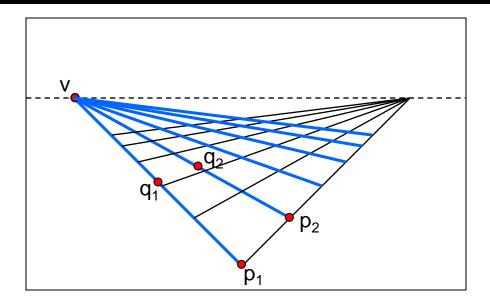
### Comparing heights



### Measuring height



### Computing vanishing points (from lines)



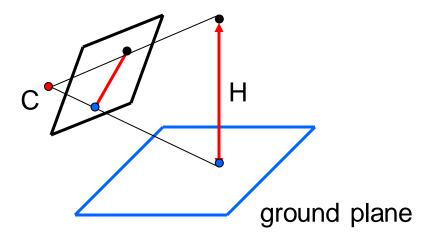
Intersect  $p_1q_1$  with  $p_2q_2$ 

$$v = (p_1 \times q_1) \times (p_2 \times q_2)$$

Least squares version

- Better to use more than two lines and compute the "closest" point of intersection
- See notes by <u>Bob Collins</u> for one good way of doing this:
  - http://www-2.cs.cmu.edu/~ph/869/www/notes/vanishing.txt

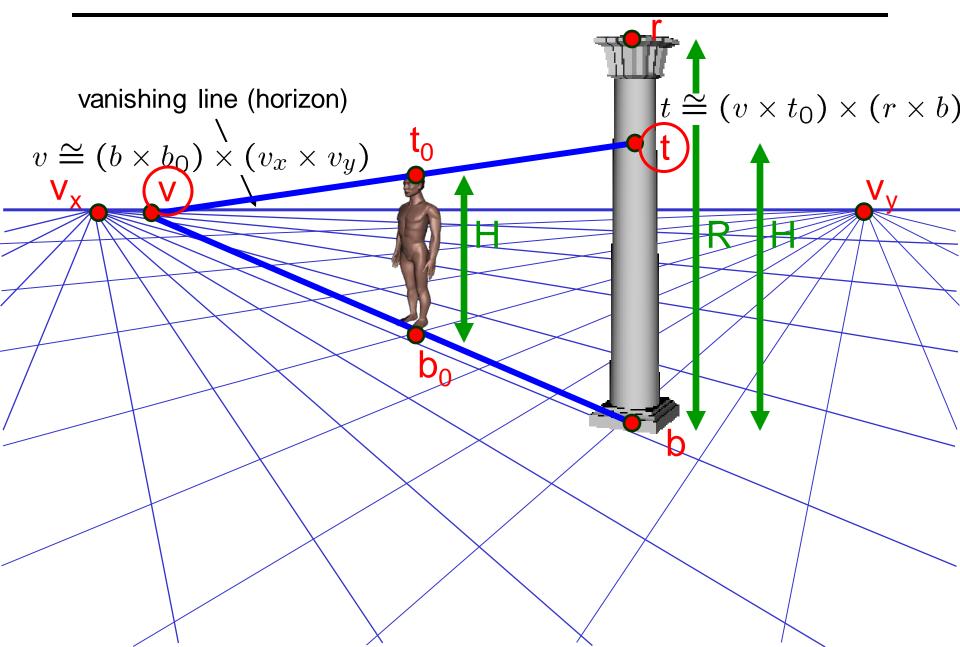
### Measuring height without a ruler



Compute H from image measurements

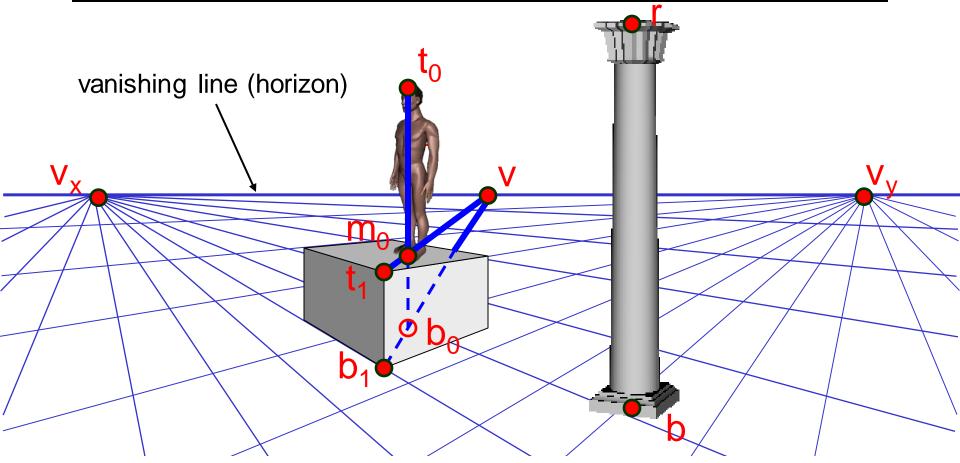
• Need more than vanishing points to do this

### Measuring height



Vz

### Measuring height



What if the point on the ground plane  $b_0$  is not known?

- Here the guy is standing on the box
- Use one side of the box to help find b<sub>0</sub> as shown above

### What if $v_z$ is not infinity?

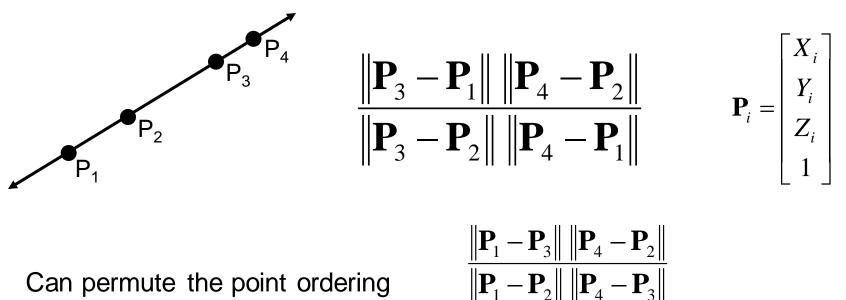


### The cross ratio

#### A Projective Invariant

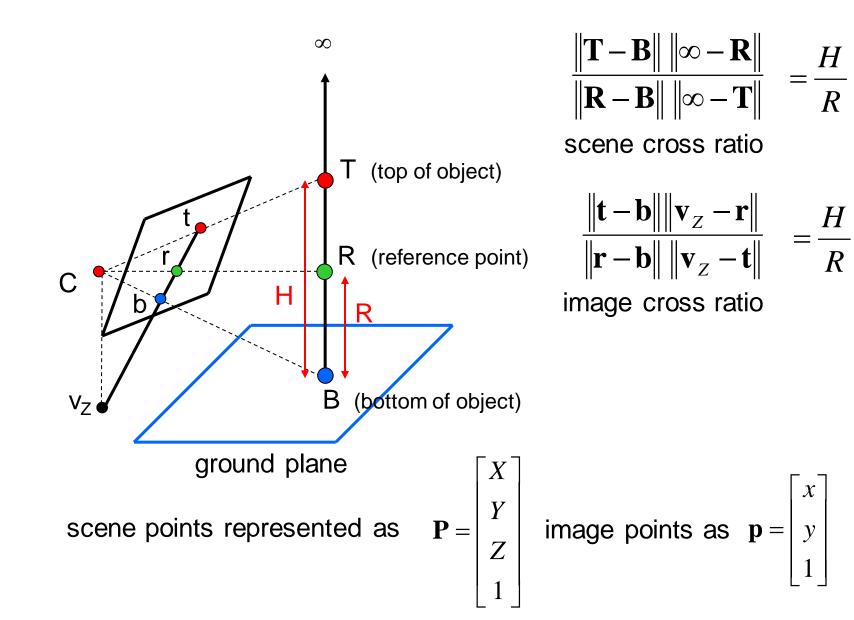
 Something that does not change under projective transformations (including perspective projection)

The cross-ratio of 4 collinear points



• 4! = 24 different orders (but only 6 distinct values) This is the fundamental invariant of projective geometry

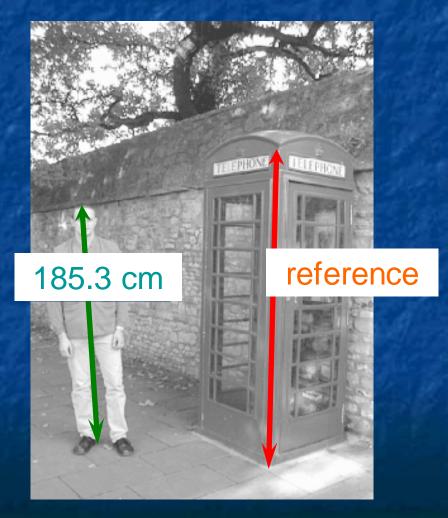
### Measuring height



### Measuring height V<sub>z</sub> vanishing line (horizon) It n V Hr Ζ $|\mathbf{V}_Z|$ Ŕ r b image cross ratio

# Measuring heights in real photos

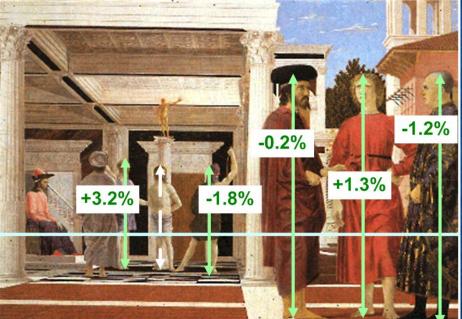
Problem: How tall is this person?



### Assessing geometric accuracy

Problem: Are the heights of the two groups of people consistent with each other?





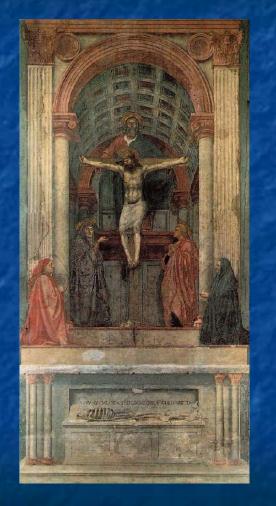
Piero della Francesca, *Flagellazione di Cristo*, c.1460, Urbino

#### Measuring relative heights

### Single-View Metrology

# Complete 3D reconstructions from single views

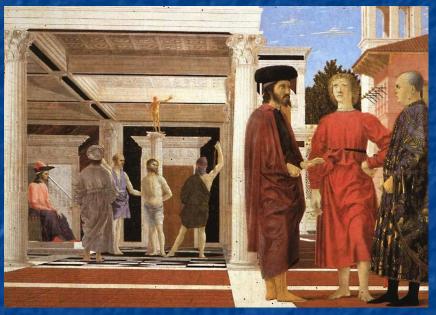
# Example: The Virtual Trinity





Masaccio, *Trinita'*, 1426, Florence

### **Example: The Virtual Flagellation**



Piero della Francesca, Flagellazione di Cristo, c.1460, Urbino



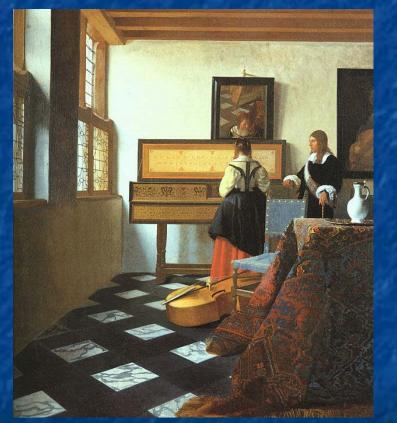
## Example: The Virtual St. Jerome



Henry V Steenwick, *St.Jerome in His Study*, 1630, The Netherlands



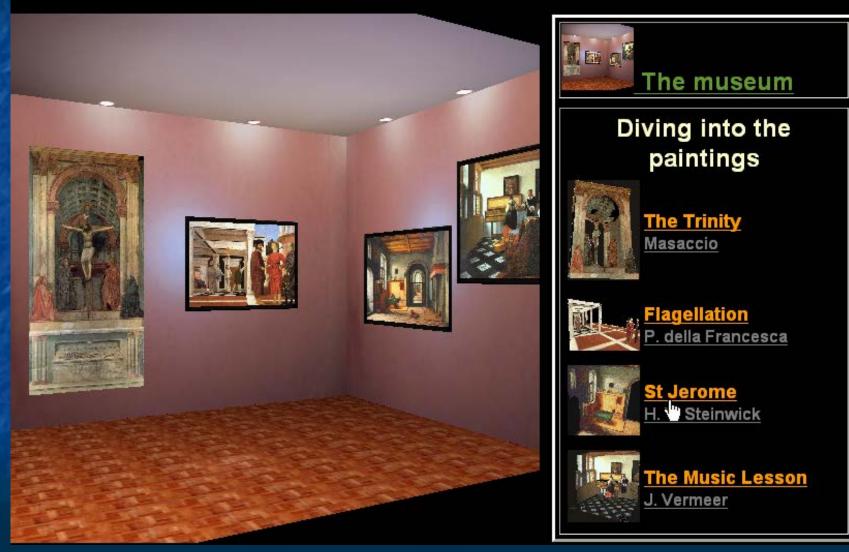
### Example: The Virtual Music Lesson





J. Vermeer, *The Music Lesson*, 1665, London

### Example: A Virtual Museum @ Microsoft A dive into the paintings third dimension



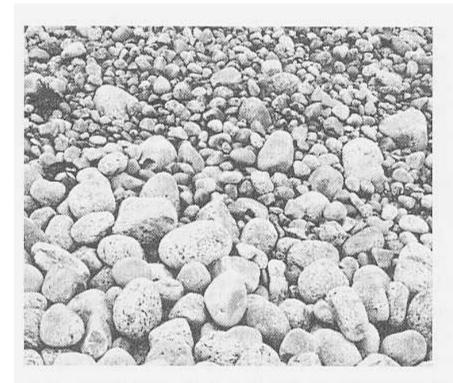
The Image-Based Realities team @ Microsoft Research

# References

**Antonio Criminisi Accurate Visual Reconstruction** from Single and Multiple **Uncalibrated Images** (Springer-Verlag) ISBN: 1-85233-468-1

look for it on amazon.com !

www.research.microsoft.com/~antcrim



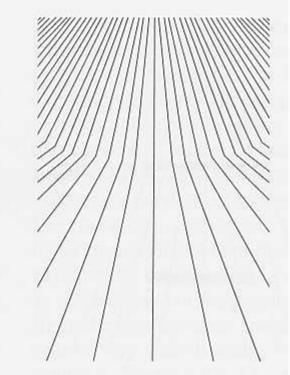
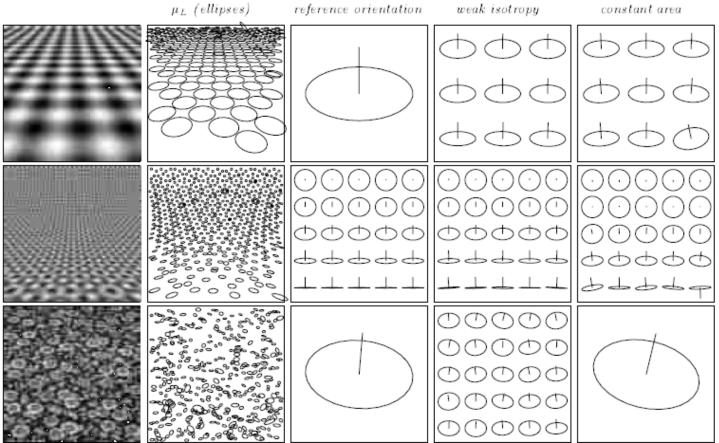


FIGURE 8.27 Texture gradients provide information about depth. (Frank Siteman/Stock, Boston.) © Frank Sitman/Stock Boston

FIGURE 8.28 Texture discontinuity signals the pre corner.

A Witkin. Recovering Surface Shape and Orientation from Texture (1981)





Shape from Texture from a Multi-Scale Perspective. Tony Lindeberg and Jonas Garding. ICCV 93

• Filter outputs

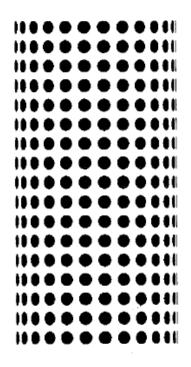
• Textons

#### Shape from Texture Using Local Spectral Moments

Boaz J. Super, Member, IEEE, and Alan C. Bovik, Senior Member, IEEE

Abstract-We present a non-feature-based solution to the problem of computing the shape of curved surfaces from texture information. First, the use of local spatial-frequency spectra and their moments to describe texture is discussed and motivated. A new, more accurate method for measuring the local spatialfrequency moments of an image texture using Gabor elementary functions and their derivatives is presented. Also described is a technique for separating shading from texture information, which makes the shape-from-texture algorithm robust to the shading effects found in real imagery. Second, a detailed model for the projection of local spectra and spectral moments of any surface reflectance patterns (not just textures) is developed. Third, the conditions under which the projection model can be solved for the orientation of the surface at each point are explored. Unlike earlier non-feature-based, curved surface shape-from-texture approaches, the assumption that the surface texture is isotropic is not required; surface texture homogeneity can be assumed instead. The algorithm's ability to operate on anisotropic and nondeterministic textures, and on both smooth- and rough-textured surfaces, is demonstrated.

Index Items—Shape from texture, shape recovery, surface orientation, moments, wavelet, spatial frequency, Gabor functions, texture, projection.



#### PLANAR SURFACE ORIENTATION FROM TEXTURE SPATIAL FREQUENCIES

BOAZ J. SUPER \*† and ALAN C. BOVIK ‡

# Assumptions:

- Smooth closed surface
- Homogeneous texture
- (sometimes, isotropic texture)

#### **Texture description**

Use filter outputs to measure local spatial frequency.

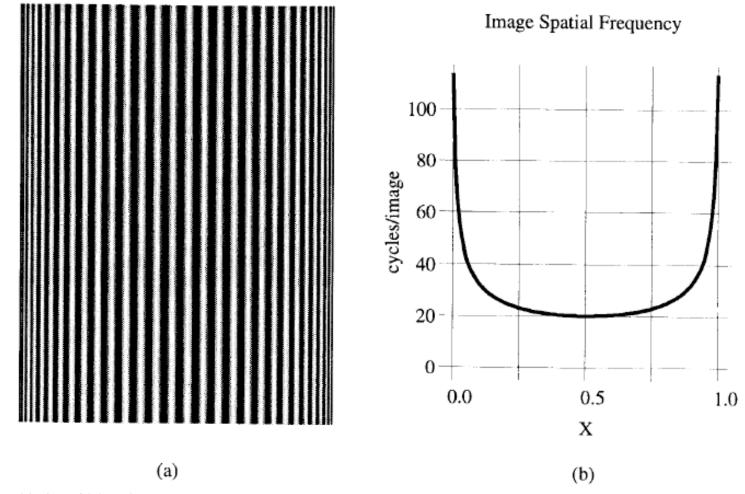


Fig. 2. (a) Cylinder with sinusoidal grating texture. (b) Horizontal component of image spatial frequency on center cross-section of (a).

#### **Texture projection**

Assume orthographic projection.

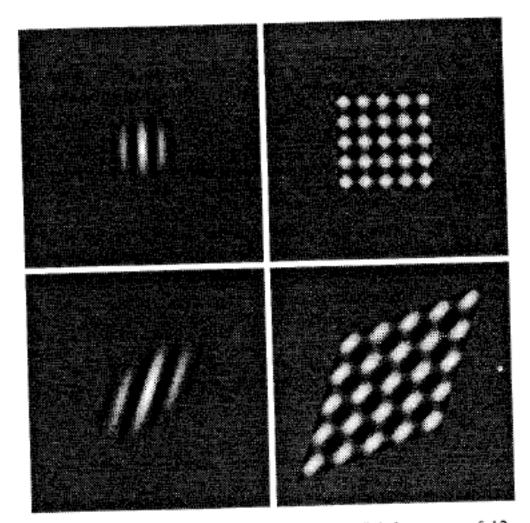
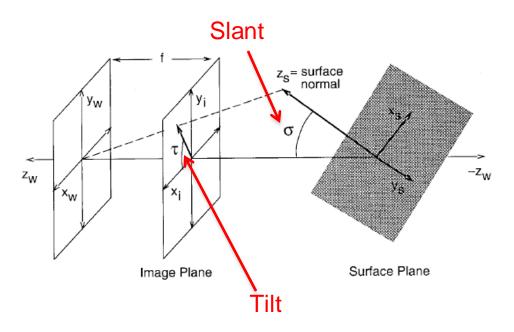
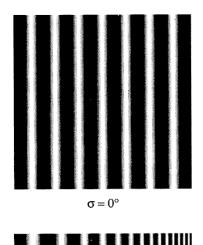


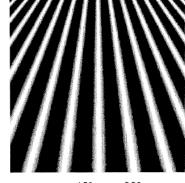
Fig. 5. Top row: real part of Gabor filter with radial frequency of 12 cycles/image, and a texture patch. Bottom row: back-projections of Gabor filter and texture patch onto a plane with orientation  $(\sigma, \tau) = (60^\circ, 45^\circ)$ .

# Slant and tilt





 $\sigma=45^{\rm o}$  ,  $\tau=0^{\rm o}$ 



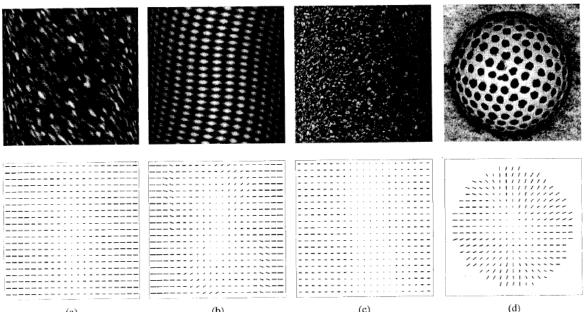




 $\sigma=45^\circ$  ,  $\tau=45^\circ$ 

#### Box 1. Summary of algorithm

- 1. Convolve the image with Gabor functions and their partial derivatives, and smooth the filter output amplitudes (to reduce noise) by convolving them with a Gaussian.
- 2. Select the Gabor filter  $h_k$  with the largest amplitude output at each point.
- 3. Compute the (signed) instantaneous frequency  $\mathbf{u}_i(\mathbf{x}_i)$  at each point using equation (6).
- 4. Sample ( $\sigma$ ,  $\tau$ )-space, backprojecting  $\mathbf{u}_i(\mathbf{x}_i)$  to compute  $\mathbf{u}_s(\mathbf{x}_s)$  using equation (20). Compute the variance  $V_{\sigma,\tau}$  of  $\mathbf{u}_s(\mathbf{x}_s)$ . Coarse-to-fine sampling in multiple stages may be used.
- 5. Output the values of  $(\sigma, \tau)$  for which  $V_{\sigma,\tau}$  is a minimum.



(b)

(a)

#### Recovering shape and irradiance maps from rich dense texton fields

Anthony Lobay and D.A. Forsyth CVPR 04

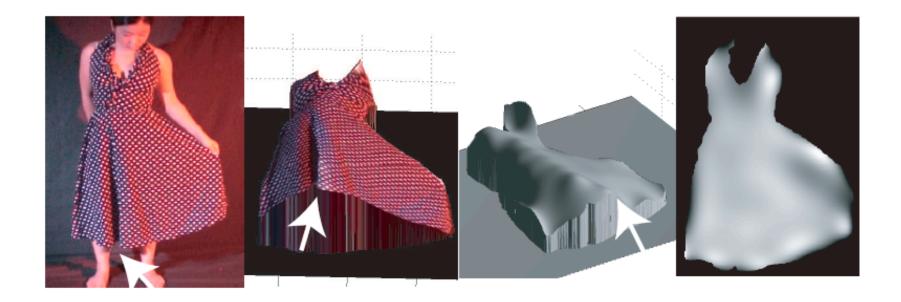


Figure 3: On the left, a view of a model in a spotted dress. In the center left, a textured view of the reconstruction obtained using our method. This reconstruction used 1200 texton instances, in 8 clusters. Note the relatively fine detail that was obtained by the reconstruction, including the two main folds in the skirt (indicated with arrows). Typically, rendering texture on top of the view produces a better looking surface, so we show the surface without texturing on the center right; arrows indicate the reconstructed folds in the geometry. Notice that the fold in the skirt is well represented. The smoothing term is generally good at resolving normal ambiguities, but patches of surface that are not well connected to the main body can be subjected to a concave-convex ambiguity, as has happened to part of the skirt's bodice here. On the right, the irradiance map estimated using our method.

#### **Texture description**

Non-occluded textons, and approximated as flat.

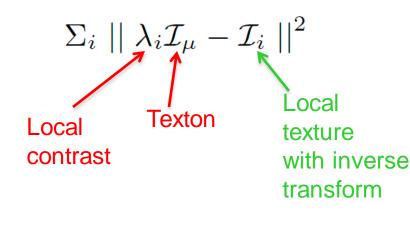


# The two pieces of the solution

If we knew the transformations

- We can find the textons
- We can find the local intensity contrast

By minimization of:



# If we knew the texton and contrast

 Recover the transformation by transforming the texton to match each local patch.

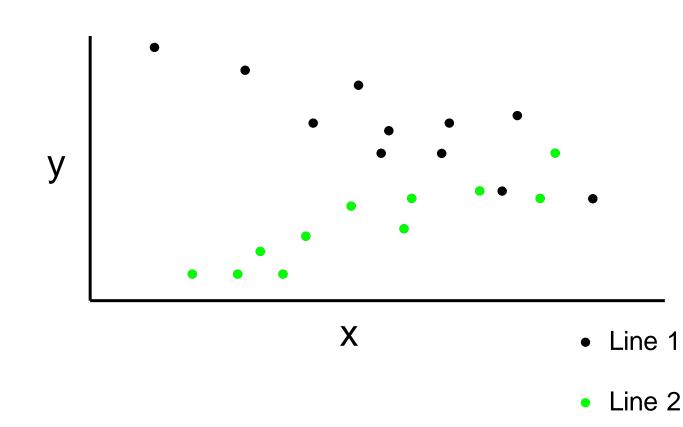
# Expectation Maximization (EM): a solution to chicken-and-egg problems



# Model fitting example Fitting two lines to observed data



## Fitting two lines: on the one hand...



If we knew which points went with which lines, we'd be back at the single linefitting problem, twice.

# Maximum likelihood estimation for the slope of a single line

data: 
$$(X_n, Y_n), n = 1 \dots, N$$
  
model:  $Y = aX + w$   
where  $w \sim N(\mu = 0, \sigma = 1)$ .

y · · · · · ·

Data likelihood for point n:

$$P(X_n, Y_n|a) = c \exp[-(Y_n - aX_n)^2/2]$$

Maximum likelihood estimate:

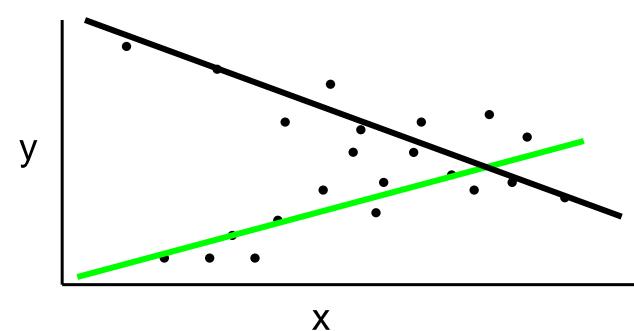
$$\hat{a} = rg\max_a p(Y_1, \dots, Y_n | a) = rg\max_a \sum_n -d(Y_n; a)^2/2$$

where 
$$d(Y_n;a) = |Y_n - aX_n|$$

gives regression formula

$$\hat{a} = \frac{\sum_{n} Y_{n} X_{n}}{\sum_{n} X_{n}^{2}}.$$
<sup>67</sup>

### Fitting two lines, on the other hand...



We could figure out the probability that any point came from either line if we just knew the two equations for the two lines.

### MLE with hidden/latent variables: Expectation Maximisation

General problem:

$$y = (Y_1, \dots, Y_N); \ \theta = (a_1, a_2); \ z = (z_1, \dots, z_N)$$

data parameters hidden variables

For MLE, want to maximise the log likelihood

The sum over z inside the log gives a complicated expression for the ML solution.

$$\hat{\theta} = \arg \max_{\theta} \log p(y|\theta)$$
  
= arg max <sub>$\theta$</sub>  log  $\sum_{z} p(y, z|\theta)$ 

### Maximizing the log likelihood of the data

if you knew the z<sub>n</sub> labels for each sample n:

$$\hat{\theta} = \operatorname{argmax}_{\theta} \sum_{n} \delta(z_n = 1) \log p(y_n \mid z_n = 1, \theta) + \delta(z_n = 2) \log p(y_n \mid z_n = 2, \theta)$$

### Maximizing the log likelihood of the data

if you knew the z<sub>n</sub> labels for each sample n:

$$\hat{\theta} = \operatorname{argmax}_{\theta} \sum_{n} \delta(z_n = 1) \log p(y_n \mid z_n = 1, \theta) + \delta(z_n = 2) \log p(y_n \mid z_n = 2, \theta)$$

In the EM algorithm, we replace those known labels with their expectation under the current algorithm parameters. So

$$E[\delta(z_n = i)] = p(z_n = i \mid y, \theta_{old})$$
  
Call that quantity  
$$= \alpha_i(n)$$
$$\propto p(y \mid z_n = i, \theta_{old}) \propto e^{-(y_n - a_i x_n)^2/2}$$

### Maximizing gives

And then for the estimate of the line parameters, we have

$$\hat{\theta} = \operatorname{argmin}_{\theta} \sum_{n} \alpha_{1}(n) (y_{n} - a_{1}x_{n})^{2} + \alpha_{2}(n) (y_{n} - a_{2}x_{n})^{2}$$

and maximising that gives

$$\hat{a}_i = \frac{\sum_n \alpha_i(n) y_n x_n}{\sum_n \alpha_i(n) x_n^2}$$

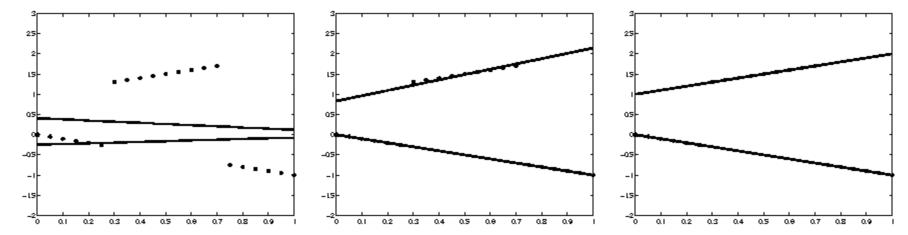
### EM fitting to two lines

with 
$$\alpha_i(n) \propto e^{-(y_n - a_i x_n)^2/2}$$
  
and  $\alpha_1(n) + \alpha_2(n) = 1$ 
  
Regression becomes:  $\hat{a}_i = \frac{\sum_n \alpha_i(n) y_n x_n}{\sum_{i=1}^n \alpha_i(n) y_n x_n}$ 
"M-step"

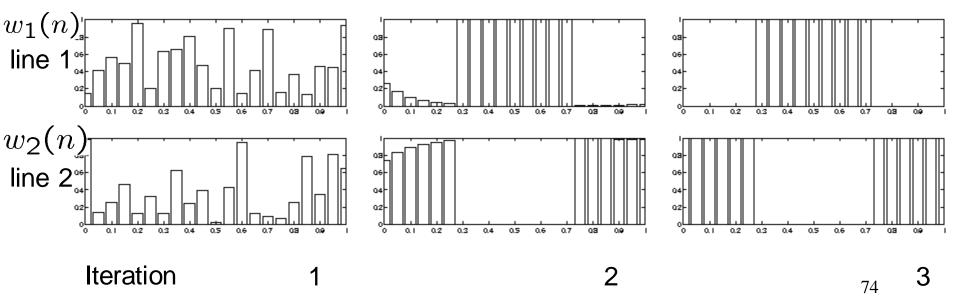
$$\hat{a}_i = \frac{\sum_n \alpha_i(n) y_n x_n}{\sum_n \alpha_i(n) x_n^2} \quad \text{"M}$$

### Experiments: EM fitting to two lines

(from a tutorial by Yair Weiss, http://www.cs.huji.ac.il/~yweiss/tutorials.html)



Line weights

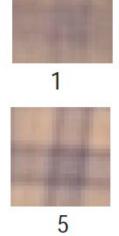


$$EM_{\frac{1}{2\sigma_{im}^2}\sum_i \left(||\lambda_i \mathcal{I}_{\mu} - \mathcal{T}_i^{-1} \mathcal{I}||^2 \delta_i\right) + \sum_i (1 - \delta_i) K + \frac{1}{2\sigma_{light}^2} (\lambda_i - 1)^2 + L$$

EM iterations

#### Find interest points







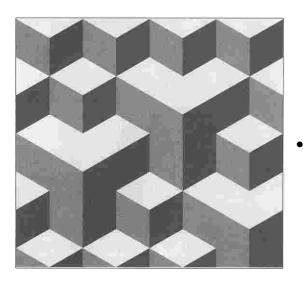
10

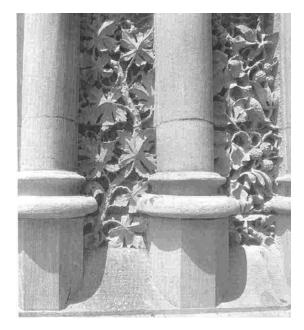




# Shading

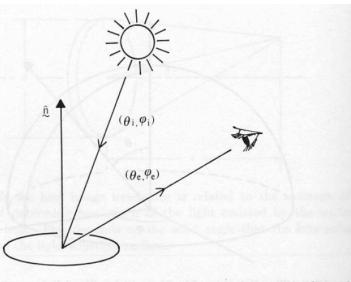
 Based on 3 dimensional modeling of objects in light, shade and shadows.





Perception of depth through shading alone is always subject to the concave/convex inversion. The pattern shown can be perceived as stairsteps receding towards the top and lighted from above, or as an overhanging structure lighted from below.

### **Reflectance** map



#### Horn, 1986

**Figure 10-7.** The bidirectional reflectance distribution function is the ratio of the radiance of the surface patch as viewed from the direction  $(\theta_e, \phi_e)$  to the irradiance resulting from illumination from the direction  $(\theta_i, \phi_i)$ .

$$BRDF = f(\theta_i, \phi_i, \theta_e, \phi_e) = \frac{L(\theta_e, \phi_e)}{E(\theta_i, \phi_i)}$$

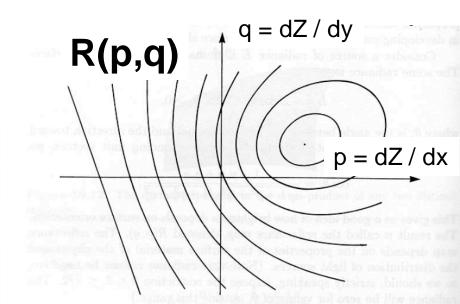
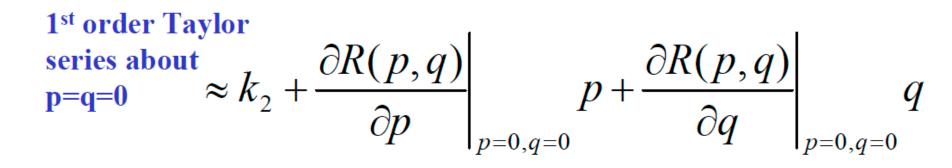


Figure 10-13. The reflectance map is a plot of brightness as a function of surface orientation. Here it is shown as a contour map in gradient space. In the case of a Lambertian surface under point-source illumination, the contours turn out to be nested conic sections. The maximum of R(p,q) occurs at the point  $(p,q) = (p_s,q_s)$ , found inside the nested conic sections, while R(p,q) = 0 all along the line on the left side of the contour map.

### Linear shape from shading

Lambertian point source

$$R(p,q) = k \frac{1 + p_s p + q_s q}{\sqrt{1 + p^2 + q^2} \sqrt{1 + p_s^2 + q_s^2}}$$



 $=k_2(1+p_sp+q_sq)$ 

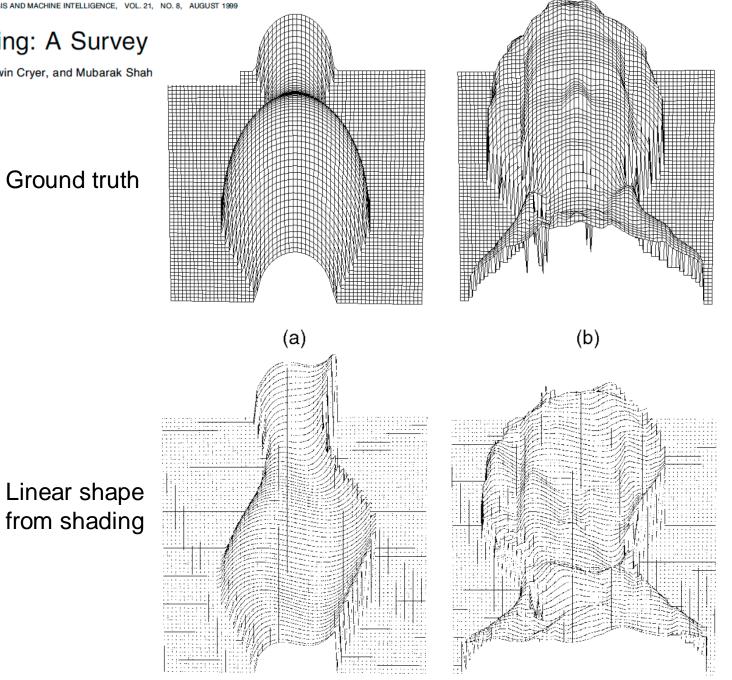
A close form solution can be obtained using the Fourier transform (Pentland 88)

$$\frac{\partial}{\partial x} Z(x, y) \longleftrightarrow F_Z(\omega_1, \omega_2)(-i\omega_1)$$
 Pentland 88

#### Shape from Shading: A Survey

Ruo Zhang, Ping-Sing Tsai, James Edwin Cryer, and Mubarak Shah

#### Ground truth



(b)

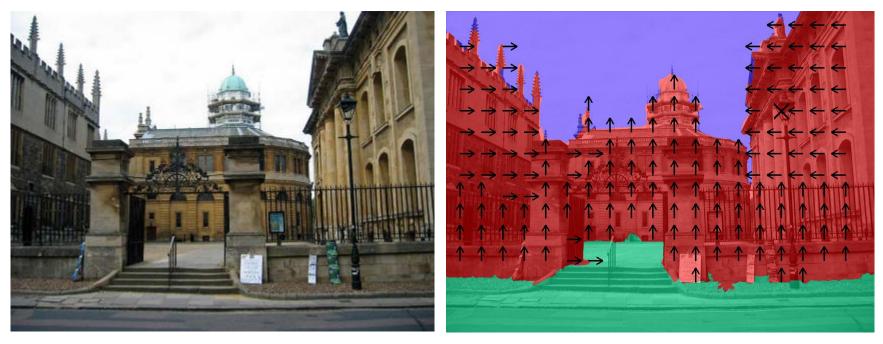
(a)

## Learning based methods

 User recognition to learn structure of the world from labeled examples



### Label Geometric Classes



- Goal: learn labeling of image into 7 Geometric Classes:
- Support (ground)
- Vertical
  - Planar: facing Left ( $\leftarrow$ ), Center (), Right ( $\rightarrow$ )
  - Non-planar: **Solid (X)**, **Porous** or wiry **(O)**
- Sky

### What cues to use?



Vanishing points, lines



Color, texture, image location



Texture gradient Slides by Efros

### Dataset very general



























## The General Case (outdoors)

- Typical outdoor photograph off the Web
  - Got 300 images using Google Image Search keyboards: "outdoor", "scenery", "urban", etc.
- Certainly not random samples from world
  - 100% horizontal horizon
  - 97% pixels belong to 3 classes -- ground, sky, vertical (gravity)
  - Camera axis usually parallel to ground plane
- Still very general dataset!

### Let's use many weak cues

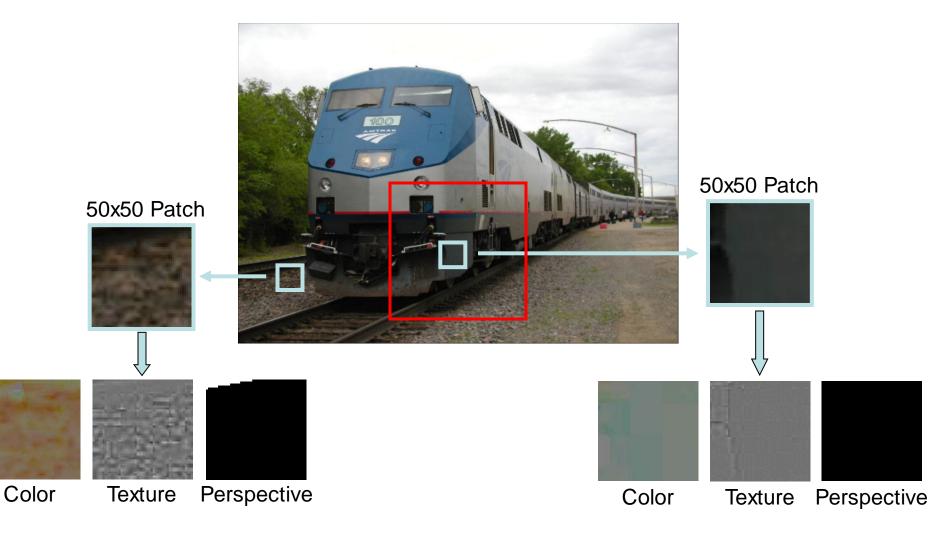
### Material

Image Location

• Perspective

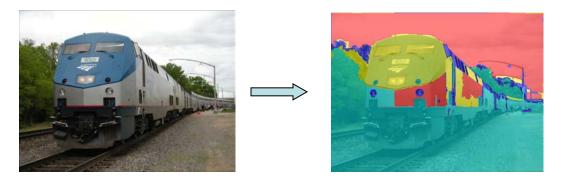
SURFACE CUES
Location and Shape
L1. Location: normalized x and y, mean
L2. Location: norm. x and y, $10^{th}$ and $90^{th}$ pctl
L3. Location: norm. y wrt estimated horizon, 10 <sup>th</sup> , 90 <sup>th</sup> pctl
L4. Location: whether segment is above, below, or straddles estimated horizon
L5. Shape: number of superpixels in segment
L6. Shape: normalized area in image
Color
C1. RGB values: mean
C2. HSV values: C1 in HSV space
C3. Hue: histogram (5 bins)
C4. Saturation: histogram (3 bins)
Texture
T1. LM filters: mean abs response (15 filters)
T2. LM filters: hist. of maximum responses (15 bins)
Perspective
P1. Long Lines: (num line pixels)/sqrt(area)
P2. Long Lines: % of nearly parallel pairs of lines
P3. Line Intersections: hist. over 8 orientations, entropy
P4. Line Intersections: % right of center
P5. Line Intersections: % above center
P6. Line Intersections: % far from center at 8 orientations
P7. Line Intersections: % very far from center at 8 orientations
P8. Vanishing Points: (num line pixels with vertical VP membership)/sqrt(area)
P9. Vanishing Points: (num line pixels with horizontal VP membership)/sqrt(area)
P10. Vanishing Points: percent of total line pixels with vertical VP membership
P11. Vanishing Points: x-pos of horizontal VP - segment center (0 if none)
P12. Vanishing Points: y-pos of highest/lowest vertical VP wrt segment center
P13. Vanishing Points: segment bounds wrt horizontal VP
P13. Vanishing Points: segment bounds with horizontal VP P14. Gradient: x, y center of gradient mag. wrt. image center Slides by Efro

### **Need Spatial Support**



## **Image Segmentation**

• Naïve Idea #1: segment the image



### - Chicken & Egg problem

• Naïve Idea #2: <u>multiple</u> segmentations



- Decide later which segments are good Slides by Efros

## Estimating surfaces from segments

- We want to know:
  - Is this a good (coherent) segment?

P(good segment | data)

- If so, what is the surface label?

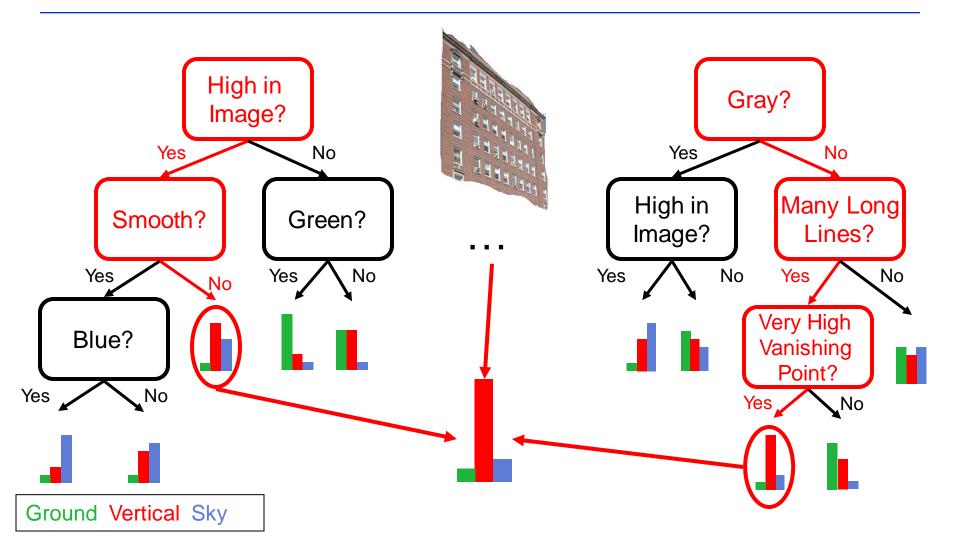
P(label | good segment, data)

 Learn these likelihoods from training images

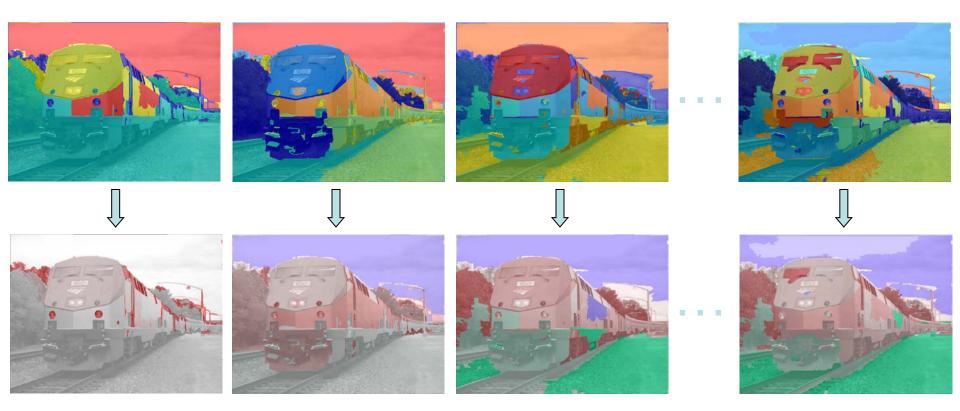
 we use Boosted Decision Trees



### **Boosted Decision Trees**



## Labeling Segments



For each segment:

- Get P(good segment | data) P(label | good segment, data)

## Image Labeling

### Labeled Segmentations

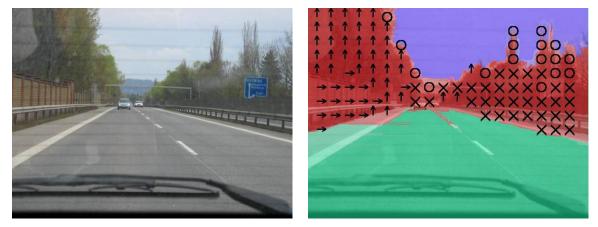






Labeled Pixels

### **No Hard Decisions**



Support







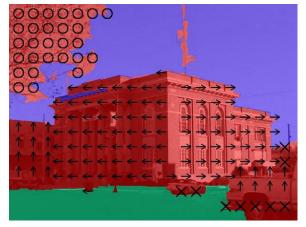


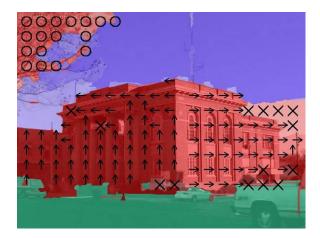




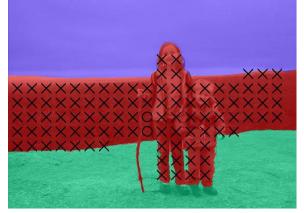
V-Left

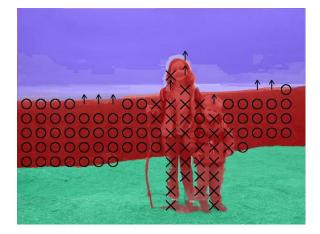








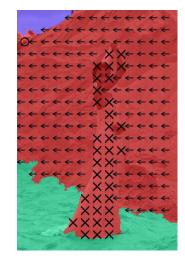


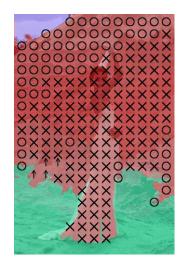


Input image

Ground Truth

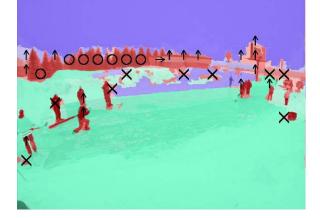






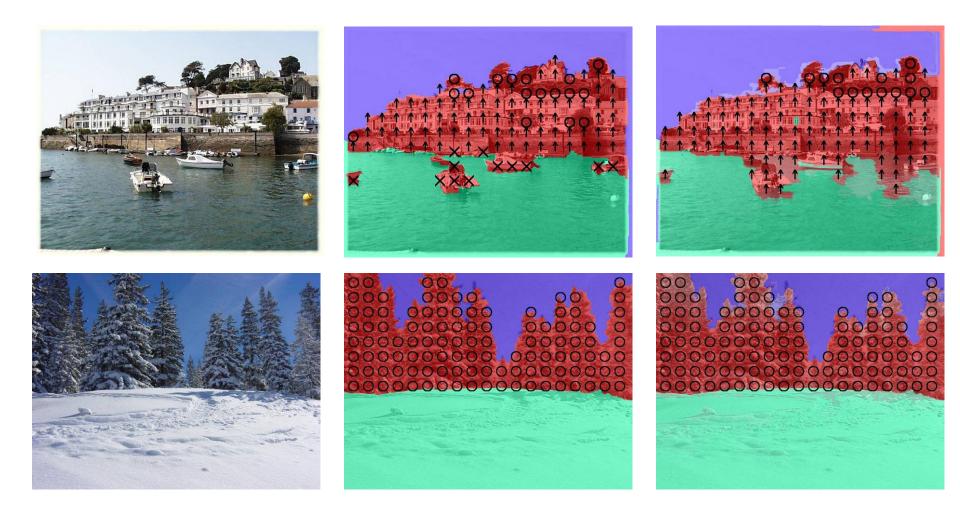






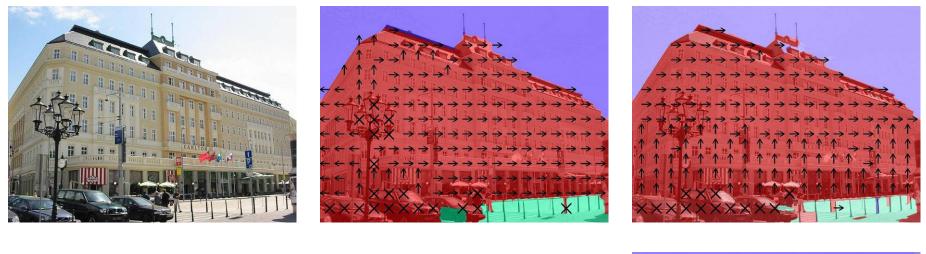
Input image

Ground Truth



Input image

Ground Truth









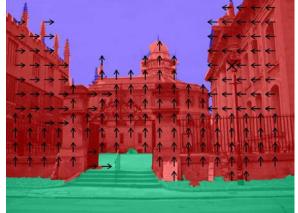
Input image

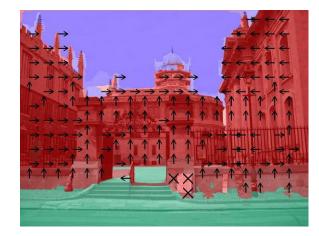
Ground Truth

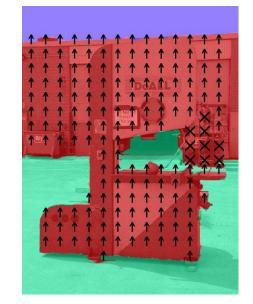




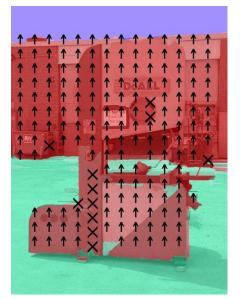
Input image

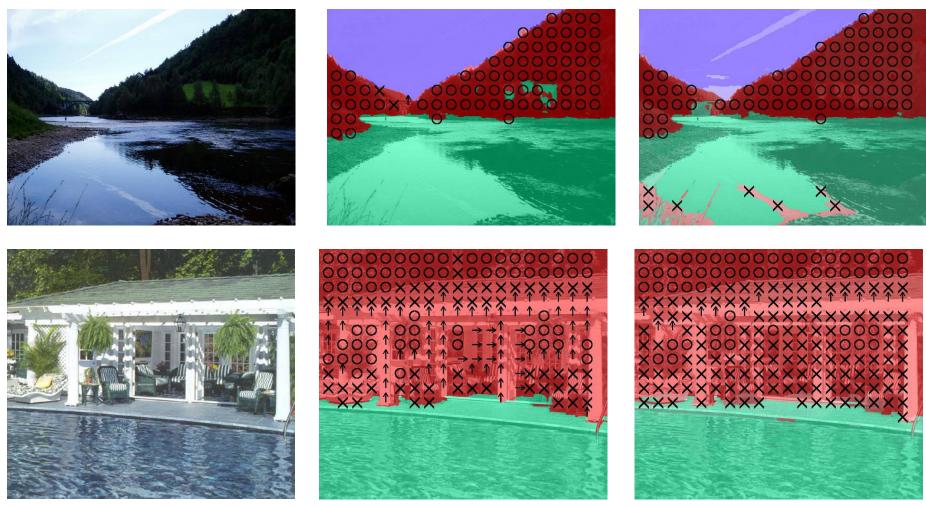






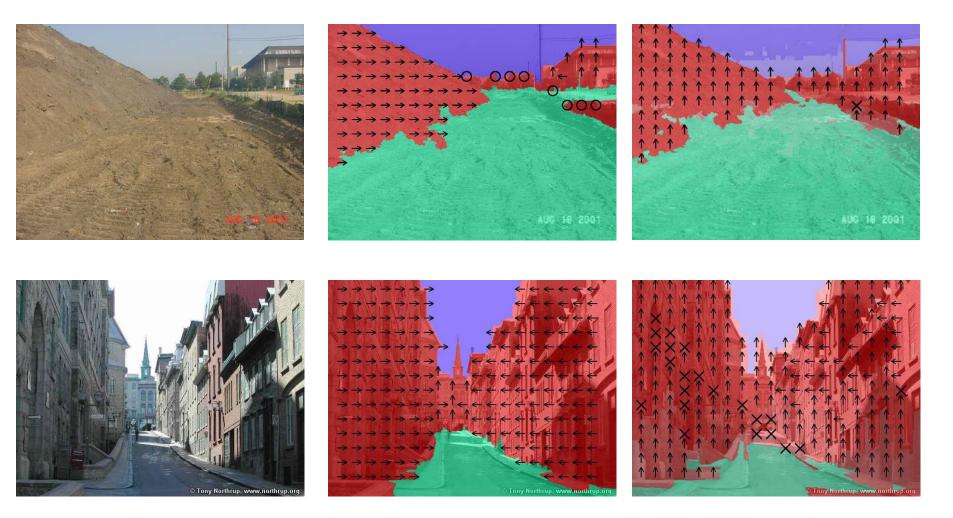
Ground Truth





Input image

Ground Truth

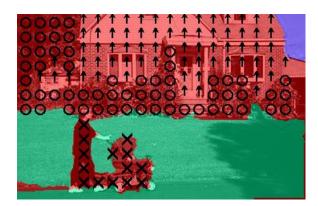


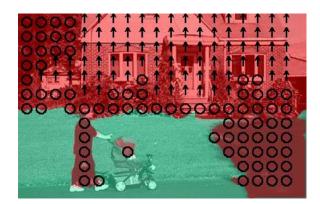
Input image

Ground Truth

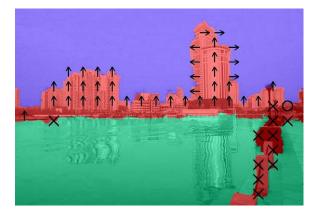
### Some Failures

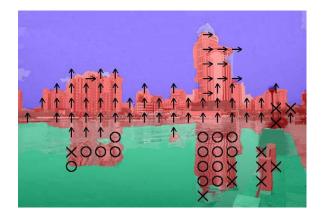








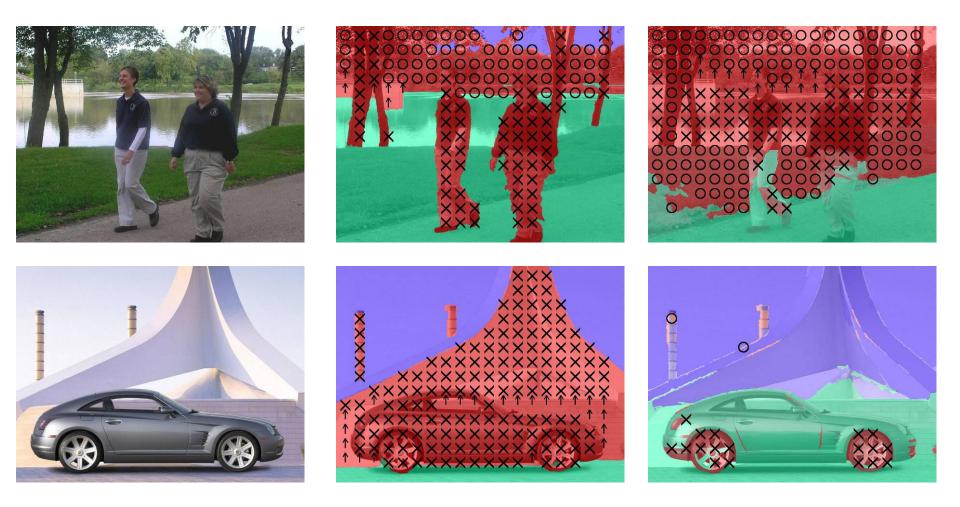




Input image

Ground Truth

### **Catastrophic Failures**



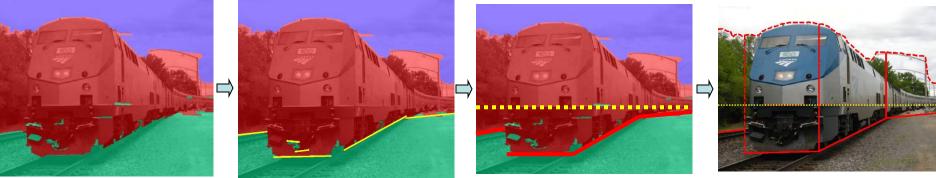
Input image

Ground Truth

### Automatic Photo Popup

Labeled Image

Fit Ground-Vertical Boundary with Line Segments Form Segments into Polylines Cut and Fold



Final Pop-up Model



[Hoiem Efros Hebert 2005]