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MIT CSAIL

6.869: Advances in Computer Vision

MIT COMPUTER VISION

Lecture 5

Statistical Image Models

Bayesian approach Use P(a, b | y = 1) = k P(y=1|a, b) P(a, b)



Statistical modeling of images



$$C(\Delta x, \Delta y) = \rho \left[\mathbf{I}(x + \Delta x, y + \Delta y), \mathbf{I}(x, y) \right]$$

Gaussian model

We want a distribution that captures the correlation structure typical of natural images.

Let **C** be the covariance matrix of the image

$$p(\mathbf{I}) = \exp\left(-\frac{1}{2}\mathbf{I}^T\mathbf{C}^{-1}\mathbf{I}\right) \qquad C = \begin{bmatrix} c_0 & c_1 & c_2 & \cdots & c_{n-1} \\ c_{n-1} & c_0 & c_1 & c_2 & \vdots \\ & c_{n-1} & c_0 & c_1 & \ddots \\ \vdots & \ddots & \ddots & \ddots & c_2 \\ & & & & c_1 \\ c_1 & \cdots & c_{n-1} & c_0 \end{bmatrix}$$

Stationarity assumption: Symmetrical circulant matrix

Diagonalization of circulant matrices: $C = EDE^{T}$

The eigenvectors are the Fourier basis

The eigenvalues are the squared magnitude of the Fourier coefficients



Statistical modeling of images

A small neighborhood

Image

Intensity histogram [1 -1] filter output [1 -1] output histogram



A model for the distribution of filter outputs



Note: this is not a good model for ALL filter outputs

Generalized Gaussian

$$p(x) = \frac{\exp(-|x/s|^r)}{2s/r\Gamma(1/r)}$$



Uniform distribution r -> infinite

The wavelet marginal model



The wavelet marginal model



k x,y

Steerable Pyramid

We may combine Steerability with Pyramids to get a Steerable Laplacian Pyramid as shown below

Decomposition

Reconstruction



Steerable Pyramid

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Decomposition

Reconstruction



Sampling images

Gaussian model



Fig. 3. Example image randomly drawn from the Gaussian spectral model, with $\gamma = 2.0$.

Wavelet marginal model



Fig. 6. A sample image drawn from the wavelet marginal model, with subband density parameters chosen to fit the image of Fig. 7.



Fig. 5. Example basis functions derived by optimizing a marginal kurtosis criterion [see 35].

Denoising

White

noise

Noisy image







Let x = bandpassed image value before adding noise. Let y = noise-corrupted observation.



Let x = bandpassed image value before adding noise.

Let y = noise-corrupted observation.





Let x = bandpassed image value before adding noise.

Let y = noise-corrupted observation.





y = 25





For small y: probably it is due to noise and y should be set to 0 For large y: probably it is due to an image edge and it should be kept untouched

MAP estimate, \hat{x} , as function of observed coefficient value, y



Figure 2: Bayesian estimator (symmetrized) for the signal and noise histograms shown in figure 1. Superimposed on the plot is a straight line indicating the identity function.

http://www-bcs.mit.edu/people/adelson/pub_pdfs/simoncelli_noise.pdf

Simoncelli and Adelson, Noise Removal via Bayesian Wavelet Coring original



With Gaussian noise of std. dev. 21.4 added, giving PSNR=22.06



(1) Denoised withGaussian model,PSNR=27.87





(2) Denoisedwith waveletmarginal model,PSNR=29.24

http://www.cns.nyu.edu/pub/eero/simoncelli05a-preprint.pdf

Gaussian scale mixtures



Fig. 7. Amplitudes of multi-scale wavelet coefficients for the "Einstein" image. Each subimage shows coefficient amplitudes of a subband obtained by convolution with a filter of a different scale and orientation, and subsampled by an appropriate factor. Coefficients that are spatially near each other within a band tend to have similar amplitudes. In addition, coefficients at different orientations or scales but in nearby (relative) spatial positions tend to have similar amplitudes. Note correlations between the amplitudes of each wavelet subband.

http://www.cns.nyu.edu/pub/eero/simoncelli05a-preprint.pdf

Statistics of pairs of wavelet coefficients

Contour plots of the joint histogram of various wavelet coefficient pairs



Conditional distributions of the corresponding wavelet pairs Fig. 8. Empirical joint distributions of wavelet coefficients associated with different pairs of basis functions, for a single

Fig. 8. Empirical joint distributions of wavelet coefficients associated with different pairs of basis functions, for a single image of a New York City street scene (see Fig. 1 for image description). The top row shows joint distributions as contour plots, with lines drawn at equal intervals of log probability. The three leftmost examples correspond to pairs of basis functions at the same scale and orientation, but separated by different spatial offsets. The next corresponds to a pair at adjacent scales (but the same orientation, and nearly the same position), and the rightmost corresponds to a pair at orthogonal orientations (but the same scale and nearly the same position). The bottom row shows corresponding conditional distributions: brightness corresponds to frequency of occurance, except that each column has been independently rescaled to fill the full range of intensities. "http://www.cns.nyu.edu/pub/eero/simoncelli05a-preprint.pdf



z is a spatially varying hidden variable
that can be used to
(a) Create the non-gaussian histograms
from a mixture of Gaussian densities, and
(b) model correlations between the
neighboring wavelet coefficients.

(d) Simulated

Fig. 9. Comparison of statistics of coefficients from an example image subband (left panels) with those generated by simulation of a local GSM model (right panels).

(c) Observed

original



With Gaussian noise of std. dev. 21.4 added, giving PSNR=22.06



(1) Denoised withGaussian model,PSNR=27.87



Separating reflections from a single image using local features

Anat Levin



Figure 1: (a) Original input image (constructed by summing the two images in b). (b) the correct decomposition. (c)-(g) alternative possible decompositions. Why should the decomposition in (b) be favored?

Assaf Zomet Yair Weiss

very simple cost function: it favors decompositions which have a small number of edges and corners. Surprisingly, this simple cost function gives the "right" decompositions for challenging real images.¹



Figure 2: An input image and some decompositions

Applications

• Detecting fake images

• Camera shake removal





Visual Worlds







Prof. Hany Farid, Dartmouth University

How do you tell if an image is fake?











Actress And Anti-War Activist Jane Fonda Speaks to a crowd of Vietnam Veterans as Activist and former Vietnam Vet John Kerry (LEFT) listens and prepares to speak next concerning the war in Vietnam (AP Photo)

http://www.cs.dartmouth.edu/farid/publications/deception09.pdf http://www.cs.dartmouth.edu/farid/publications/significance06.pdf

The source images



Update: Fonda, Kerry and Photo Fakery (free reg. required) – Photographer Ken Light describes the experience of discovering his 1970 photograph of John Kerry circulating in altered form on the Internet. "As far as I know, John Kerry never shared a demonstration podium with Jane Fonda, and the fact that a widely circulated photo showed him doing so — until it was exposed in recent weeks as a hoax — tells us more about the troublesome combination of Photoshop and the Internet than it does about the prospective Democratic candidate for president." (*Washington Post*) IEEE Transactions on Signal Processing, 53(2):845-850, 2005

How Realistic is Photorealistic?

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Abstract—Computer graphics rendering software is capable of generating highly photorealistic images that can be impossible to differentiate from photographic images. As a result, the unique stature of photographs as a definitive recording of events is being diminished (the ease with which digital images can be manipulated is, of course, There has been some work in evaluating the photorealism of computer graphics rendered images from a human perception point of view (e.g., [10], [9], [11]). To our knowledge, however, no computational techniques exist to differentiate between photographic and photorealistic images (a method for differentiating between photo

Input image



Representation of color input image in wavelet subbands





Filter bank

Separable Quadrature Mirror Filters





Each output is called subband

Histograms of wavelet subband coefficients



mean (μ), variance (μ_2), skewness (μ_3/σ^3), kurtosis (μ_4/σ^4)
There are correlations between subband coefficients







Figure 2.10: A natural image (left) and the histograms of the linear prediction errors of coefficient magnitudes for all subbands in a three-scale QMF pyramid decomposition of the image on the left.

Hypothesis: there is something different in the correlation between wavelet coefficients between real images and computer generated images.

Summary of features used for image classification





Projection of measured features into a 3-d space: well separated even in that low-dimensional space



noise fractal discs natural

Photographic training set: downloaded from www.freefoto.com





















Photorealistic training set: downloaded from www.raph.com and www.irtc.org



















photorealistic (6,000)

Classifier 1: LDA. Simple, amenable to analysis



linear discriminant analysis (LDA)

Classifier 2: SVM. State of the art.



linear SVM

non-linear SVM

Easily classified photographic images



Fig. 4: Easily classified photographic images.

Easily classified photorealistic images



Fig. 5: Easily classified photorealistic images.

Incorrectly classified photographic images



Fig. 6: Incorrectly classified photographic images.

Incorrectly classified photorealistic images



Fig. 7: Incorrectly classified photorealistic images.

www.fakeorfoto.com







Results of algorithm

Photographic images

Photorealistic images



Fig. 9: Images from www.fakeorfoto.com. Shown in (a) and (c) are correctly and incorrectly classified photographic images, respectively. Shown in (b) and (d) are correctly and incorrectly classified photorealistic images, respectively.

Taking a picture...

What the camera give us...

(-: GIARLES HEILI W'I MALTER STUPPED

How do we correct this?

Close-up

Original

Naïve Sharpening C

Our algorithm



Why does picture appear blurry?

Let's take a photo



Blurry result



Slow-motion replay



Slides R. Fergus

Slow-motion replay





Motion of camera

Image formation process



Why is this hard?

Simple analogy: 11 is the product of two numbers. What are they?

No unique solution:

 $11 = 1 \times 11$ $11 = 2 \times 5.5$ $11 = 3 \times 3.667$ etc.....

Need more information !!!!

Multiple possible solutions



Blurry image



Natural image statistics

Characteristic distribution with heavy tails



Histogram of image gradients



Blury images have different statistics



Histogram of image gradients



Parametric distribution



Histogram of image gradients



Use parametric model of sharp image statistics Slides R. Fergus

Existing work on image deblurring

Software algorithms:

- Extensive literature in signal processing community
- Mainly Fourier and/or Wavelet based
- Strong assumptions about blur
 - \rightarrow not true for camera shake



Assumed forms of blur kernels

Image constraints are frequency-domain power-laws

Existing work on image deblurring

Hardware approaches

Image stabilizers

Dual cameras

Coded shutter







Ben-Ezra and Nayar 2004 Raskar et al. SIGGRAPH 2006

Our approach can be combined with these hardware methods

Three sources of information

1. Reconstruction constraint:



2. Image prior:



Distribution of gradients

3. Blur prior:



Positive & Sparse

Three sources of information

y = observed image b = blur kernel x = sharp image

p(b, x|y) = k p(y|b, x) p(x) p(b)Posterior 1. Likelihood 2. Image 3. Blur (Reconstruction prior prior constraint)

1. Likelihood p(y|b, x)

y = observed image b = blur x = sharp image

Reconstruction constraint:

$$p(y|b,x) = \prod_i \mathcal{N}(y_i|x_i \otimes b, \sigma^2)$$

 $\propto \prod_i e^{-rac{(x_i \otimes b - y_i)^2}{2\sigma^2}}$

i - pixel index

2. Image prior p(x)

y = observed image b = blur x = sharp image

$$p(x) = \prod_i \sum_{c=1}^C \pi_c \mathcal{N}(f(x_i)|0, s_c^2)$$

Mixture of Gaussians fit to empirical distribution of image gradients

- i pixel index
- c mixture component index
- f derivative filter



3. Blur prior p(b)

y = observed image b = blur x = sharp image

$p(b) = \prod_j \sum_{d=1}^D \pi_d \mathcal{E}(b_j | \lambda_d)$

Mixture of Exponentials

- Positive & sparse
- No connectivity constraint

- j blur kernel element
- d mixture component index



How do we use this information?

Obvious thing to do:

- Combine 3 terms into an objective function
- Run conjugate gradient descent
- This is Maximum a-Posteriori (MAP)
Results from MAP estimation



Input blurry image

Maximum a-Posteriori (MAP)



Our method: Variational Bayes



Variational Bayesian method

Based on work of Miskin & Mackay 2000



Keeps track of uncertainty in estimates of image and blur by using a distribution instead of a single estimate

Helps avoid local maxima and over-fitting

Overview of algorithm

1. Pre-processing

- 2. Kernel estimation
 - Multi-scale approach

Input image



- 3. Image reconstruction
 - Standard non-blind deconvolution routine

Preprocessing

Input image



Bayesian inference too slow to run on whole image

Infer kernel from this patch



Initialization

Input image



Inferring the kernel: multiscale method



Use multi-scale approach to avoid local minima:



Image Reconstruction



Results on real images

Submitted by people from their own photo collections Type of camera unknown

Output does contain artifacts

- Increased noise
- Ringing

Compares well to existing methods









Close-up of garland





Original

Matlab's deconvblind

Original photograph



Matlab's deconvblind



Photoshop sharpen more











Original photograph





Original photograph





Matlab's deconvblind



Original photograph



Our output



Blur kernel

Close-up of bird

Original



Unsharp mask









Image artifacts & estimated kernels

Blur kernels



Image patterns

Note: blur kernels were inferred from large image patches, NOT the image patterns shown

Bayesian methods

